

APPLICATION NO. 09/826,117

TITLE OF INVENTION: Hyhrid Walsh Codes for CDMA

INVENTOR: Urbain A. von der Embse

Marked up version of SUBSTITUTE SPECIFICATION
using the original specification of 2001

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INVENTORS: Urbain Alfred A. von der Embse

5

BACKGROUND OF THE INVENTION

10

I. Field of the Invention

TECHNICAL FIELD

The present invention relates to CDMA (Code Division
15 Multiple Access) cellular telephone and wireless data
communications with data rates up to multiple T1 (1.544 Mbps) and
higher (>100 Mbps), and to optical CDMA with data rates in the
Gbps and higher ranges. Applications are mobile, point-to-point
and satellite communication networks. More specifically the
20 present invention relates to novel complex and ~~hybrid~~ generalized
complex Walsh codes developed to replace current ~~real~~ Walsh
orthogonal CDMA channelization codes which are real Walsh codes.

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CONTENTS

<u>BACKGROUND ART</u>	page 1
<u>SUMMARY OF INVENTION</u>	page 11
<u>BRIEF DESCRIPTION OF DRAWINGS AND PERFORMANCE DATA</u>	page 13
<u>DISCLOSURE OF INVENTION</u>	page 14
<u>REFERENCES</u>	page 32
<u>DRAWINGS AND PERFORMANCE DATA</u>	page 33

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II. Description of the Related Art

BACKGROUND ART

Current CDMA art is represented by the recent work on
5 multiple access for broadband wireless communications, the G3
(third generation CDMA) proposed standard candidates, the current
IS-95 CDMA standard, the early Qualcomm patents, and the real
Walsh technology. These are documented in ~~references 1,2,3,4,5,6.~~
Reference 1 is an issue of the ~~IEEE communications magazine~~
10 ~~devoted to multiple access communications for broadband wireless~~
~~networks, reference 2 is an issue on IEEE personal communications~~
~~devoted to the third generation (3G) mobile systems in~~
~~Europe~~ "Multiple Access for Broadband Networks", IEEE
Communications magazine July 2000 Vol. 38 No. 7, "Third
15 Generation Mobile Systems in Europe", IEEE Personal
Communications April 1998 Vol. 5 No. 2, ~~reference 3 is the IS-~~
~~95/IS-95A, standard primarily developed by Qualcomm, references 4~~
~~and 5 are Qualcomm patents addressing the use of real Walsh~~
~~orthogonal CDMA codes, and reference 6 is the widely used~~
20 ~~reference on real Walsh technology. the IS-95/IS-95A, the 3G~~
CDMA2000 and W-CDMA, and the listed patents.

Current art using ~~real~~ Walsh orthogonal CDMA channelization
codes is represented by the scenario described in the following
25 with the aid of equations (1) and FIG 1,2,3,4. This scenario
considers CDMA communications spread over a common frequency band
for each of the communication channels with each channel defined
by a CDMA code. These CDMA communications channels for each of
the users are defined by assigning a unique Walsh orthogonal
30 spreading codes to each user. The Walsh code for each user
spreads the user data symbols over the common frequency band.
These Walsh encoded user signals are summed and re-spread over
the same frequency band by ~~one or more~~ long and short pseudo-noise
PN codes, to generate the CDMA communications signal which is

modulated and transmitted. The communications link consists of a transmitter, propagation path, and receiver, as well as interfaces and control.

5 It is assumed that the communication link is in the communications mode with all of the users communicating at the same symbol rate and the synchronization is sufficiently accurate and robust to support this communications mode. In addition, the possible power differences between the users is assumed to be
10 incorporated in the data symbol amplitudes prior to the CDMA encoding in the CDMA transmitter, and the power is uniformly spread over the wideband by proper selection of the CDMA pulse waveform. ~~It is self evident to anyone skilled in the CDMA communications art that these communications mode assumptions~~
15 ~~are both reasonable and representative of the current CDMA art and do not limit the applicability of this invention.~~

Transmitter equations (1) describe a representative real Walsh CDMA encoding for the transmitter in FIG. 1. It is
20 assumed that there are N Walsh code vectors $W(u)$ each of length N chips 1. The code vector is presented by a $1 \times N$ N-chip row vector $W(u) = [W(u,1), \dots, W(u,N)]$ where $W(u,n)$ is chip n of code u. The code vectors are the row vectors of the Walsh matrix W. Walsh code chip n of code vector u has the possible values
25 $W(u,n) = \pm 1$. Each user is assigned a unique Walsh code which allows the code vectors to be designated by the user symbols $u=0,1,\dots,N-1$ for N Walsh codes. User data symbols 2 are the set of complex symbols $\{Z(u), u=0,1,\dots,N-1\}$ and the set of real symbols $\{R(u_R), I(u_I), u_R, u_I=0,1,\dots,N-1\}$ where Z is a complex
30 symbol and R,I are real symbols assigned to the real, imaginary communications axis. Examples of complex user symbols are QPSK and OQPSK encoded data corresponding to 4-phase and offset 4-phase symbol coding. Examples of real user symbols are PSK and DPSK encoded data corresponding to 2-phase and differential 2-
35 phase symbol coding. Although not considered in this example, it

is possible to use combinations of both complex and real data symbols.

5 Current real Walsh CDMA encoding for transmitter (1)

1 Walsh codes

W = Walsh $N \times N$ orthogonal code matrix consisting of

N rows of N chip code vectors

 = $[W(u)]$ matrix of row vectors $W(u)$

10 = $[W(u,n)]$ matrix of elements $W(u,n)$

$W(u)$ = Walsh code vector u for $u=0,1,\dots,N-1$

 = $[W(u,0), W(u,1), \dots, W(u,N-1)]$

 = $1 \times N$ row vector of chips $W(u,0), \dots, W(u,N-1)$

$W(u,n)$ = Walsh code u chip n

15 = $+/-1$ possible values

2 Data symbols

$Z(u)$ = Complex data symbol for user u

$R(u_R)$ = Real data symbol for user u_R assigned to the

20 Real axis of the CDMA signal

$I(u_I)$ = Real data symbol for user u_I assigned to the

 Imaginary axis of the CDMA signal

3 Walsh encoded data

25 Complex data symbols

$Z(u,n) = Z(u) \text{sgn}\{ W(u,n) \}$

 = User u chip n Walsh encoded complex data

 Real data symbols

$R(u_R,n) = R(u_R) \text{sgn}\{ W(u_R,n) \}$

30 = User u_R chip n Walsh encoded

 real data

$I(u_I,n) = R(u_R) \text{sgn}\{ W(u_R,n) \}$

 = User u_I chip n Walsh encoded

 real data

35 where $\text{sgn}\{ (o) \} = \text{Algebraic sign of } "(o)"$

4 — 4 — PN scrambling

$P_2(n), P_{R2}(n), P_{I2}(n)$ = Chip n of long PN codes

$P_R(n)$ = Chip n of short PN codes for real axis

5 $P_I(n)$ = Chip n of short PN codes for imaginary ~~Axis~~axis

Complex data symbols:

$Z(n)$ = PN scrambled real Walsh encoded data chips
after summing over the users

$$\begin{aligned} 10 \quad &= \sum_u Z(u,n) P_2(n) [P_R(n) + j P_I(n)] \\ &= \sum_u Z(u,n) \text{sign}\{P_2(n)\} [\text{sgn}\{P_R(n)\} + j \text{sgn}\{P_I(n)\}] \\ &= \text{Real Walsh CDMA encoded complex chips} \end{aligned}$$

Real data symbols:

$$15 \quad Z(n) =$$

$$\begin{aligned} &[\sum_{u_R} R(u_R, n) \text{sgn}\{P_{R2}(n)\} + j \sum_{u_I} I(u_I, n) \text{sgn}\{P_{I2}(n)\}] [\text{sign}\{P_R(n)\} + j \text{sign}\{P_I(n)\}] \\ &= \text{Real Walsh CDMA encoded real chips} \end{aligned}$$

20

User data is encoded by the Walsh CDMA codes 3. Each of the user symbols $Z(u), R(u_R), I(u_I)$ is assigned a unique Walsh code. $W(u), W(u_R), W(u_I)$. Walsh encoding of each user data symbol generates an N-chip sequence with each chip in the sequence consisting of the user data symbol with the sign of the corresponding Walsh code chip, which means each chip = [Data symbol] x [Sign of Walsh chip].

30 The Walsh encoded data symbols are summed and encoded with PN codes 4. These long PN codes are 2-phase with each chip equal to ± 1 which means PN encoding consists of sign changes with each sign change corresponding to the sign of the PN chip. Short PN codes are complex with 2-phase codes along their real

and imaginary axes. Encoding with a long PN means each chip of the summed Walsh encoded data symbols has a sign change when the corresponding long PN chip is -1, and remains unchanged for +1 values. This operation is described by a multiplication of each chip of the summed Walsh encoded data symbols with the sign of the PN chip. Purpose of the PN encoding ~~for complex data symbols~~ is to provide scrambling of the summed Walsh encoded data symbols as well as isolation between groups of users and synchronization. PN encoding uses a long PN which is real followed by a short PN which is complex with real code components on the inphase and quadrature axes as shown in 4. ~~Purpose of the separate PN encoding for the real and imaginary axes is to provide approximate orthogonality between the real and imaginary axes, since the same Walsh orthogonal codes are being used for these axes. Another PN encoding can be used as illustrated in these equations for the combined real and imaginary CDMA signals to provide scrambling and isolation between groups of users.~~

Receiver equations (2) describe a representative ~~real~~-Walsh CDMA decoding for the receiver in FIG. 3. The receiver front end 5 provides estimates $\{\hat{Z}(n) = \hat{R}(n) + j\hat{I}(n)\}$ of the transmitted real Walsh CDMA encoded chips $\{Z(n) = R(n) + jI(n)\}$ for the complex and real data symbols. Orthogonality property 6 is expressed as a matrix product of the ~~real~~-Walsh code chips or equivalently as a matrix ~~produce~~-product of the Walsh code chip numerical signs. ~~The 2-phase PN codes 7 have the useful decoding property that the square of each code chip is unity which is equivalent to observing that the square of each code chip numerical sign is unity.~~ Decoding algorithms 8 perform the inverse of the signal processing for the encoding in equations (1) to recover estimates $\{\hat{Z}(u)\}$ or $\{\hat{R}(u_R), \hat{I}(u_I)\}$ of the transmitter user symbols $\{Z(u)\}$ or $\{R(u_R), I(u_I)\}$ for the respective complex or real data symbols.

Current real Walsh CDMA decoding for receiver (2)

5 Receiver front end provides estimates $\{\hat{Z}(n) = \hat{R}(n) + j\hat{I}(n)\}$
of the encoded transmitter chip symbols $\{Z(n) = R(n) + jI(n)\}$
for the complex and real data symbols

6 Orthogonality property of ~~real~~ Walsh NxN matrix W

$$\sum_n W(\hat{u}, n) W(n, u) = \sum_n \text{sign}\{W(\hat{u}, n)\} \text{sign}\{W(n, u)\} \\ = N \delta(\hat{u}, u)$$

10 where $\delta(\hat{u}, u)$ = Delta function of \hat{u} and u
= 1 for $\hat{u} = u$
= 0 otherwise

7 PN decoding property:

$$\frac{P_2(n) P_2(n)}{\text{sgn}\{P_2(n)\} \text{sgn}\{P_2(n)\}} = 1$$

15

Decoding algorithm:

Complex data symbols

$$\hat{Z}(u) =$$

$$2^{-1} N^{-1} \sum_n \hat{Z}(n) [\text{sgn}\{P_2(n)\} [\text{sgn}\{P_R(n)\} - j \text{sgn}\{P_I(n)\}] \text{sgn}\{W(n, u)\}]$$

20

= Receiver estimate of the transmitted complex
data symbol Z(u)

Real data symbols

$$\hat{R}(u_R) =$$

25

$$\text{Real}[2^{-1} N^{-1} \sum_n \hat{Z}(n) [\text{sgn}\{P_R(n)\} - j \text{sgn}\{P_I(n)\}] \text{sgn}\{P_2(n)\} \text{sgn}\{W(n, u_R)\}]$$

= Receiver estimate of the transmitted complex
data symbol R(u_R)

$$\hat{I}(u_I) =$$

30

$$\text{Imag}[2^{-1}N^{-1} \sum_n \hat{Z}(n) [\text{sgn}\{P_R(n)\} - j\text{sgn}\{P_I(n)\}] \text{sgn}\{P_2(n)\} \text{sgn}\{W(n, u_I)\}]$$

= Receiver estimate of the transmitted complex
data symbol $I(u_I)$

5

FIG. 1 CDMA transmitter block diagram is representative of a current CDMA transmitter which includes an implementation of the current real Walsh CDMA channelization encoding in equations (1). This block diagram becomes a representative implementation of the CDMA transmitter which implements the ~~new-complex~~ Walsh CDMA encoding of this invention disclosure when the current real Walsh CDMA encoding 13 is replaced by the ~~new-complex~~ Walsh CDMA encoding of this invention. Signal processing starts with the stream of user input data words 9. Frame processor 10 accepts these data words and performs the encoding and frame formatting, and passes the outputs to the symbol encoder 11 which encodes the frame symbols into amplitude and phase coded symbols 12 which could be complex $\{Z(u)\}$ or real $\{R(u_R), I(u_I)\}$ depending on the application. These symbols 12 are the inputs to the current real Walsh CDMA encoding in equations (1). Inputs $\{Z(u)\}, \{R(u_R), I(u_I)\}$ 12 are ~~real~~ Walsh encoded, summed over the users, and scrambled by PN in the current ~~real~~ Walsh CDMA encoder 13 to generate the complex output chips $\{Z(n)\}$ 14. This encoding 13 is a representative implementation of equations (1). These output chips $Z(n)$ are waveform modulated 15 to generate the analog complex signal $z(t)$ which is single sideband upconverted, amplified, and transmitted (Tx) by the analog front end of the transmitter 15 as the real waveform $v(t)$ 16 at the carrier frequency f_0 whose amplitude is the real part of the complex envelope of the baseband waveform $z(t)$ multiplied by the carrier frequency and the phase angle ϕ accounts for the phase change from the baseband signal to the transmitted signal.

~~It should be obvious to anyone skilled in the communications art that this example implementation in FIG. 1 clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.~~

FIG. 2 real Walsh CDMA encoding is a representative implementation of the ~~real~~ Walsh CDMA encoding 13 in FIG. 1 and in equations (1). Inputs are the user data symbols which could be complex $\{Z(u)\}$ or real $\{R(u_R), +jI(u_I)\}$ 17. For complex and real data symbols the encoding of each user by the corresponding Walsh code is described in 18 by the implementation of transferring the sign of each Walsh code chip to the user data symbol followed by a 1-to-N expander 1¹N of each data symbol into an N chip sequence using the sign transfer of the Walsh chips.

For complex data symbols $\{Z(u)\}$ the sign-expander operation 18 generates the N-chip sequence $Z(u,n) = Z(u) \text{sgn}\{W(u,n)\} = Z(u)W(u,n)$ for $n=0,1,\dots,N-1$ for each user $u=0,1,\dots,N-1$. This Walsh encoding serves to spread each user data symbol into an orthogonally encoded chip sequence which is spread over the CDMA communications frequency band. The Walsh encoded chip sequences for each of the user data symbols are summed over the users 19 followed and encoded by PN encoding with a long code $P_2(n)$ with followed by a short code the scrambling sequences $[P_R(n)+jP_I(n)]$ 21. ~~PN encoding is implemented by transferring the sign of each PN chip to the summed chip of the Walsh encoded data symbols.~~ Output is the stream of complex CDMA encoded chips $\{Z(n)\}$ 22. The switch 20 selects the appropriate signal processing path for the complex and real data symbols.

For real data symbols $\{R(u_R), +jI(u_I)\}$ the real and imaginary communications axis data symbols are separately Walsh

encoded 18, summed 19, and then PN encoded 19 with long codes $P_{R2}(n)$ for the real axis and $P_{I2}(n)$ for the imaginary axis to provide orthogonality between the channels along the real and imaginary communications axes. Output is complex combined 19 and PN encoded with the ~~scrambling~~ short PN sequence $[P_R(n) + jP_I(n)]$ 21. Output is the stream of complex CDMA encoded chips $\{Z(n)\}$ 22.

~~It should be obvious to anyone skilled in the communications art that this example implementation in FIG. 2 clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.~~

FIG. 3 CDMA receiver block diagram is representative of a current CDMA receiver which includes an implementation of the current real Walsh CDMA decoding in equations (2). This block diagram becomes a representative implementation of the CDMA receiver which implements the ~~new~~ complex Walsh CDMA decoding when the current real Walsh CDMA decoding 27 is replaced by the ~~new~~ complex Walsh CDMA decoding of this invention. FIG. 3 signal processing starts with the user transmitted wavefronts incident at the receiver antenna 23 for the n_u users $u = 1, \dots, n_u \leq N_c$. These wavefronts are combined by addition in the antenna to form the receive (Rx) signal $\hat{v}(t)$ at the antenna output 23 where $\hat{v}(t)$ is an estimate of the transmitted signal $v(t)$ 16 in FIG. 1, that is received with errors in time Δt , frequency Δf , phase $\Delta \theta$, and with an estimate $\hat{z}(t)$ of the transmitted complex baseband signal $z(t)$ 16 in FIG. 1. This received signal $\hat{v}(t)$ is amplified and downconverted by the analog front end 24 and then synchronized (synch.) and analog-to-digital (ADC) converted 25. Outputs from the ADC are filtered and chip detected 26 by the

fullband chip detector, to recover estimates $\{\hat{Z}(n) = \hat{R}(n) + j\hat{I}(n)\}$ 28 of the transmitted signal which is the stream of complex CDMA encoded chips $\{Z(n)=R(n)+jI(n)\}$ 14 in FIG. 1 for both complex and real data symbols. The CDMA decoder 27 implements the 5 algorithms in equations (2) by stripping off the PN code(s) and decoding the received CDMA real Walsh orthogonally encoded chips to recover estimates $\{\hat{Z}(u) = \hat{R}(u_R) + j\hat{I}(u_I)\}$ 29 of the transmitted user data symbols $\{Z(u) = R(u_R) + jI(u_I)\}$ 12 in FIG. 1. Notation introduced in FIG. 1 and 3 assumes that the user index 10 $u=u_R=u_I$ for complex data symbols, and for real data symbols the user index u is used for counting the user pairs (u_R, u_I) of real and complex data symbols. These estimates are processed by the symbol decoder 30 and the frame processor 31 to recover estimates 32 of the transmitted user data words.

15 ~~It should be obvious to anyone skilled in the communications art that this example implementation clearly defines the fundamental current CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.~~

FIG. 4 real Walsh CDMA decoding is a representative implementation of the real Walsh CDMA decoding 27 in FIG. 3 and 25 in equations (2). Inputs are the received estimates of the complex CDMA encoded chips $\{\hat{Z}(n)\}$ 33. The PN scrambling codes ~~is~~ are stripped off from these chips 34 by ~~changing the sign of each chip according to~~ multiplying by the numerical sign of the real and imaginary components of the complex conjugate of the PN 30 code as per the decoding algorithms ~~8-7~~ in equations (2).

For complex data symbols 35 the long PN code is stripped off and the real Walsh channelization coding is removed by a

pulse compression operation consisting of multiplying each received chip by the numerical sign of the corresponding Walsh chip for the user, scaling by $1/2N$, and summing the products over the N Walsh chips **36** to recover estimates $\{\hat{Z}(u)\}$ of the user complex data symbols $\{Z(u)\}$. The switch **35** selects the appropriate signal processing path for the complex and real data symbols.

For real data symbols **35** the next signal processing operation is the removal of the remaining PN codes from the real and imaginary axes. This is followed by stripping off the ~~real~~ Walsh channelization coding by multiplying each received chip by the numerical sign of the corresponding Walsh chip for the user, scaling by $1/2N$, and summing the products over the N Walsh chips **36** to recover estimates $\{\hat{R}(u_R), \hat{I}(u_I)\}$ of the user real data symbols $\{R(u_R), I(u_I)\}$.

It should be obvious to anyone skilled in the communications art that ~~this—these~~ these example implementations clearly defines the fundamental current CDMA signal processing relevant to this invention disclosure and it is obvious that ~~this—these~~ examples ~~is—~~ are representative of the other possible signal processing approaches.

For cellular applications the transmitter description describes the transmission signal processing applicable ~~to—of~~ this invention for both the hub and user terminals, and the receiver describes the corresponding receiving signal processing for the hub and user terminals for applicability ~~to—of~~ this invention.

SUMMARY OF THE INVENTION

~~SUMMARY OF INVENTION~~

5 This invention is a new approach to the application of Walsh orthogonal codes for CDMA, which offers to replaces the current real Walsh codes with ~~the new complex Walsh codes~~ called hybrid Walsh codes and ~~the hybrid generalized complex Walsh codes~~ called generalized hybrid Walsh codes. ~~disclosed in~~
10 ~~this invention.~~ Real Walsh codes are used for current CDMA applications ~~and will be used for all of the future CDMA systems.~~ This invention ~~of~~ and complex Walsh codes will provide the choice of using ~~the new complex Walsh codes~~ or the real Walsh codes since the permuted real Walsh codes are the real
15 components of the complex Walsh codes. This means an application capable of using the complex Walsh codes can simply turn-off the complex axis components of the complex Walsh codes for real Walsh CDMA coding and decoding.

20 The complex Walsh codes of this invention are proven to be the natural development for the Walsh codes and therefore are the correct complex Walsh codes to within arbitrary factors that include scale and rotation, which are not relevant to performance. This natural development of the complex Walsh codes
25 in the N-dimensional complex code space C^N extended the correspondences between the real Walsh codes and the Fourier codes in the N-dimensional real code space R^N , to correspondences between the complex Walsh codes and the discrete Fourier transform (DFT) complex codes in C^N .

30 These ~~new~~ 4-phase complex Walsh orthogonal CDMA codes provide fundamental performance improvements compared to the 2-phase real Walsh codes which include an increase in the carrier-to-noise ratio (CNR) for data symbol recovery in the receiver,
35 lower correlation side-lobes under timing offsets both with and

without PN spreading, lower levels of harmonic interference caused by non-linear amplification of multi-carrier CDMA signals, and reduced phase tracking jitter for code tracking to support both acquisition and synchronization. These potential performance
5 improvements simply reflect the widely known principle that complex CDMA is better than real CDMA.

The ~~new hybrid generalized~~ complex Walsh orthogonal CDMA codes increase the choices for the code length by allowing the
10 combined use of ~~complex hybrid~~ Walsh, Walsh, and discrete Fourier transform complex orthogonal codes using a Kronecker or tensor construction, direct sum construction, as well as the possibility for more general functional combining.

15

~~BRIEF DESCRIPTION OF DRAWINGS AND PERFORMANCE DATA~~

BRIEF DESCRIPTION OF THE DRAWINGS AND THE PERFORMANCE DATA

20

The above-mentioned and other features, objects, design algorithms, implementations, and performance advantages of the present invention will become more apparent from the detailed description set forth below when taken in conjunction with the
25 drawings and performance data wherein like reference characters and numerals denote like elements, and in which:

FIG. 1 is a representative CDMA transmitter signal processing implementation block diagram, with emphasis on the
30 current real Walsh CDMA encoding which contains the signal processing elements addressed by this invention disclosure.

FIG. 2 is a representative CDMA encoding signal processing implementation diagram with emphasis on the current real Walsh

CDMA encoding which contains the signal processing elements addressed by this invention disclosure.

FIG. 3 is a representative CDMA receiver signal processing implementation block diagram, with emphasis on the current real Walsh CDMA decoding which contains the signal processing elements addressed by this invention disclosure.

FIG. 4 is a representative CDMA decoding signal processing implementation diagram, with emphasis on the current real Walsh CDMA decoding which contains the signal processing elements addressed by this invention disclosure.

FIG. 5 is a representative correlation plot of the correlation between the complex discrete Fourier transform (DFT) cosine and sine code component vectors and the real Fourier transform cosine and sine code component vectors.

FIG. 6 is a representative CDMA encoding signal processing implementation diagram with emphasis on the ~~new-complex-hybrid~~ Walsh CDMA encoding which contains the signal processing elements addressed by this invention disclosure

FIG. 7 is a representative CDMA decoding signal processing implementation diagram with emphasis on the ~~new-hybrid~~ Walsh CDMA decoding which contains the signal processing elements addressed by this invention disclosure.

~~DISCLOSURE OF INVENTION~~

DISCLOSURE OF THE INVENTION

5 ~~Consider the Real-real orthogonal CDMA code space R^N for~~
Hadamard, Walsh, and Fourier codes~~—.~~ The new complex Walsh
orthogonal CDMA codes are called hybrid Walsh codes and are
derived from the current real Walsh codes by starting with the
correspondence of the current real Walsh codes with the discrete
10 real Fourier transform (DFT) basis vectors. ~~Consider the real~~
~~orthogonal CDMA code space R^N consisting of N orthogonal real~~
~~code vectors.~~ Examples of code sets in R^N consisting of N -
orthogonal real code vectors include the Hadamard, Walsh, and
Fourier. The corresponding matrices of code vectors are
15 designated as H, W, F respectively and as defined in equations
(~~13~~) ~~respectively~~ consist of N -rows of N -chip code vectors.
Hadamard codes in their re-ordered form known as Walsh codes are
used in the current CDMA, in the proposals for the next
generation G3 CDMA, and in the proposals for all future CDMA.
20 Walsh codes re-order the Hadamard codes according to increasing
sequency. ~~These codes assumed ± 1 values.~~ Sequency is the
average rate of change of the sign of the codes. ~~and the~~
~~reordering places the Walsh codes in correspondence to the DFT~~
~~wherein sequency is in correspondence with frequency in the DFT.~~

25 ~~It is important to note that the correspondence~~
~~"sequency-frequency" only applies to the complex DFT matrix E~~
~~consisting of the N row vectors $\{E(u) = [E(u, 0), \dots, E(u, N-1)]$~~
~~wherein the elements of E are $E(u, n) = e^{j(2\pi un/N)}$, $u, n = 0, 1, \dots, N-1$.~~
30 ~~Historically it has not been applied to the Fourier basis F in~~
 ~~R^N .~~

Equations (~~13~~) define the three sets H, W, F of real
orthogonal codes in R^N with the understanding that the H and W
35 are identical except for the ordering of the code vectors.

Hadamard 37 and Walsh 38 orthogonal functions are basis vectors in R^N and are used as code vectors for orthogonal CDMA channelization coding. Hadamard 37 and Walsh 38 equations of definition are widely known, ~~with examples given in Reference~~
 5 ~~[6]~~. Likewise, the Fourier 39 equations of definition are widely known within the engineering and scientific communities, wherein

10 N-chip real orthogonal CDMA codes (3)

37 Hadamard codes

H = Hadamard $N \times N$ orthogonal code matrix
 consisting of N rows of N chip code vectors

15

= [$H(u)$] matrix of row vectors $H(u)$
 = [$H(u,n)$] matrix of elements $H(u,n)$

$H(u)$ = Hadamard code vector u
 = [$H(u,0), H(u,1), \dots, H(u,N-1)$]
 20 = $1 \times N$ row vector of chips $H(u,0), \dots, H(u,N-1)$

$H(u,n)$ = Hadamard code u chip n
 = $+/-1$ possible values

$$= (-1)^{\sum_{i=0}^{M-1} u_i n_i}$$

where $u = \sum_{i=0}^{M-1} u_i 2^i$ binary representation of u

25

$$n = \sum_{i=0}^{M-1} n_i 2^i \text{ binary representation of } n$$

38 Walsh codes

W = Walsh $N \times N$ orthogonal code matrix consisting of
 N rows of N chip code vectors

30

= [$W(u)$] matrix of row vectors $W(u)$
 = [$W(u,n)$] matrix of elements $W(u,n)$

$$W(u) = \text{Walsh code vector } u$$

$$= [W(u,0), W(u,1), \dots, W(u,N-1)]$$

$$W(u,n) = \text{Walsh code } u \text{ chip } n$$

$$= +/ - 1 \text{ possible values}$$

$$= (-1)^{[u_{M-1}n_0 + \sum_{i=1}^{M-1} (u_{M-1-i} + u_{M-i})n_i]}$$

39 Fourier codes

$$F = \text{Fourier } N \times N \text{ orthogonal code matrix consisting of}$$

$$N \text{ rows of } N \text{ chip code vectors}$$

$$= [F(u)] \text{ matrix of row vectors } F(u)$$

$$= \begin{bmatrix} C \\ S \end{bmatrix}$$

$$C = N/2+1 \times N \text{ matrix of row vectors } C(u)$$

$$C(u) = \text{Even code vectors for } u=0,1,\dots,N/2$$

$$= [1, \cos(2\pi u_1/N), \dots, \cos(2\pi u_{(N-1)/2}/N)]$$

$$S = N/2-1 \times N \text{ matrix of row vectors } S(u)$$

$$S(\Delta u) = \text{Odd code vectors for } u=N/2+\Delta u, \Delta u=1,2,\dots,N/2-1$$

$$= [\sin(2\pi \Delta u_1/N), \dots, \sin(2\pi \Delta u_{(N-1)/2}/N)]$$

$$\text{where } F(u) = C(u) \quad \text{for } u=0,1,\dots,N/2$$

$$= S(\Delta u) \quad \text{for } \Delta u = u-N/2, u=N/2+1,\dots,N-1$$

the cosine $C(u)$ and sine $S(u)$ code vectors are the code vectors of the Fourier code matrix F .

~~Complex~~ Consider the complex orthogonal CDMA code space C^N for DFT codes. The DFT orthogonal codes are a complex basis for the complex N -dimensional CDMA code space C^N and consist of the DFT harmonic code vectors arranged in increasing order of frequency. Equations (4) are the definition of the DFT code vectors. The DFT definition 40 is widely known within the

engineering and scientific communities. Even and odd components of the DFT code vectors **41** are the real cosine code vectors $\{C(u)\}$ and the imaginary sine code vectors $\{S(u)\}$ where even and odd are referenced to the midpoint of the code vectors. These
 5 cosine and sine code vectors are the extended set $2N$ of the N Fourier cosine and sine code vectors.

10 N-chip DFT complex orthogonal CDMA codes _____ **(4)**

40 DFT code vectors

E = DFT $N \times N$ orthogonal code matrix consisting of
 N rows of N chip code vectors

= $[E(u)]$ matrix of row vectors $E(u)$

15 = $[E(u,n)]$ matrix of elements $E(u,n)$

$E(u)$ = DFT code vector u

= $[E(u,0), E(u,1), \dots, E(u,N-1)]$

= $1 \times N$ row vector of chips $E(u,0), \dots, E(u,N-1)$

$E(u,n)$ = DFT code u chip n

20 = $e^{j2\pi un/N}$

= $\cos(2\pi un/N) + j\sin(2\pi un/N)$

= N possible values on the unit circle

25 **41** Even and odd code vectors are the extended set of Fourier even and odd code vectors in **39** equations **(3)**

$C(u)$ = Even code vectors for $u=0,1,\dots,N-1$

= $[1, \cos(2\pi u 1/N), \dots, \cos(2\pi u (N-1)/N)]$

$S(u)$ = Odd code vectors for $u=0,1,\dots,N-1$

= $[0, \sin(2\pi u 1/N), \dots, \sin(2\pi u (N-1)/N)]$

30 $E(u) = C(u) + j S(u)$ for $u=0,1,\dots,N-1$

Consider the ~~Complex~~ complex orthogonal CDMA code space C^N for ~~complex~~ hybrid Walsh codes. Step 1 in the derivation of

the ~~complex~~hybrid Walsh codes in this invention establishes the correspondence of the even and odd Walsh codes with the even and odd Fourier codes. Even and odd for these codes are with respect to the midpoint of the row vectors similar to the definition for the DFT vector codes 41 in equations (4). Equations (5) identify the even and odd Walsh codes in the W basis in R^N . These even and odd Walsh codes can be placed in

10 Even and odd Walsh codes in R^N (5)

$$\begin{aligned} W_e(u) &= \text{Even Walsh code vector} \\ &= W(2u) \quad \text{for } u=0,1,\dots,N/2-1 \\ W_o(u) &= \text{Odd Walsh code vectors} \\ &= W(2u-1) \quad \text{for } u=1,\dots,N/2 \end{aligned}$$

15

direct correspondence with the Fourier code vectors 39 in equations (3) using the DFT equations (4). This correspondence is defined in equations (6) where the correspondence operator " \sim " represents the even and odd correspondence between the Walsh and Fourier codes, and additionally represents the sequency~frequency correspondence.

25 Correspondence between Walsh and Fourier codes (6)

$$\begin{aligned} W(0) &\sim C(0) \\ W_e(u) &\sim C(u) \quad \text{for } u=1,\dots,N/2-1 \\ W_o(u) &\sim S(u) \quad \text{for } u=1,\dots,N/2-1 \\ W(N-1) &\sim C(N/2) \end{aligned}$$

30

Step 2 derives the set of N complex DFT vector codes in C^N from the set of N real Fourier vector codes in R^N . This means that the set of $2N$ cosine and sine code vectors in 41 in equations (4) for the DFT codes in C^N will be derived from the

set of N cosine and sine code vectors in **39** in equations (3) for the Fourier codes in R^N . The first $N/2+1$ code vectors of the DFT basis can be written in terms of the Fourier code vectors in equations (7).

5

DFT code vectors $0, 1, \dots, N/2$ derived from Fourier _____ (7)

42 Fourier code vectors from **39** in equations (3) are

10

$$\begin{aligned} C(u) &= \text{Even code vectors for } u=0, 1, \dots, N/2 \\ &= [1, \cos(2\pi u_1/N), \dots, \cos(2\pi u_{(N-1)/N/2})] \\ S(u) &= \text{Odd code vectors for } u=1, 2, \dots, N/2-1 \\ &= [\sin(2\pi u_1/N), \dots, \sin(2\pi u_{(N1/2-1)/N})] \end{aligned}$$

15

43 DFT code vectors in **41** of equations (4) are written as functions of the Fourier code vectors

$$\begin{aligned} E(u) &= \text{DFT complex code vectors for } u=0, 1, \dots, N/2 \\ &= C(0) \\ &= C(u) + jS(u) \quad \text{for } u=1, \dots, N/2-1 \\ &= C(N/2) \quad \text{for } u=N/2 \end{aligned}$$

20

The remaining set of $N/2+1, \dots, N-1$ DFT code vectors in C^N can be derived from the original set of Fourier code vectors by a correlation which establishes the mapping of the DFT codes onto the Fourier codes. We derive this mapping by correlating the real and imaginary components of the DFT code vectors with the corresponding even and odd components of the Fourier code vectors. The correlation operation is defined in equations (8)

25

30

Correlation of DFT and Fourier code vectors (8)

$$\begin{aligned} \text{Corr}(\text{even}) &= C * \text{Real}\{E'\} \\ &= \text{Correlation matrix} \end{aligned}$$

35

= Matrix product of C^* and the real part
 of E transpose
 Corr(odd) = $S \cdot \text{Imag}\{E'\}$
 = Correlation matrix
 5 = Matrix product of S and the imaginary
 part of E transpose

wherein "*" is the matrix product, "'" is the conjugate transpose
 operator, and the results of the correlation calculations are
 10 plotted in FIG. 5 for $N=32$ for the real cosine and the odd sine
 Fourier code vectors. Plotted are the correlation of the $2N$ DFT
 cosine and sine codes against the N Fourier cosine and sine codes
 which range from -15 to $+16$ where the negative indices of the
 codes represent a negative correlation value. The plotted curves
 15 are the correlation peaks. These correlation curves in FIG. 5
 prove that the remaining $N/2+1, \dots, N-1$ code vectors of the DFT are
 derived from the Fourier code vectors by equations (9). This

20 DFT code vectors $N/2+1, \dots, N-1$ derived from Fourier (9)
 $E(u) = C(N/2 - \Delta u) - jS(N/2 - \Delta u)$
 for $u = N/2 + \Delta u$
 $\Delta u = 1, \dots, N/2-1$

25

This construction of the remaining DFT basis in equations (9) is an application of the DFT spectral foldover property which observes the DFT harmonic vectors for frequencies $f_{NT} = N/2 + \Delta i - u$ above the Nyquist sampling rate $f_{NT} = N/2$ simply foldover such that the DFT harmonic vector for $f_{NT} = N/2 + \Delta i - u$ is the DFT basis vector for $f_{NT} = N/2 - \Delta i - u$ to within a fixed sign and where "f" is frequency and "T" is sample interval.
~~fixed phase angle of rotation.~~

Step 3 derives the ~~complex-hybrid~~ Walsh code vectors from the real Walsh code vectors by using the DFT derivation in equations (7) and (9), by using the correspondences between the real Walsh and Fourier in equations (6), and by using the fundamental correspondence between the ~~complex-hybrid~~ Walsh and the complex DFT given in equation (10).

Correspondence between ~~complex-hybrid~~ Walsh and DFT (10)

$\tilde{W} \sim E = N \times N$ complex DFT orthogonal code matrix
 where
 $\tilde{W} = N \times N$ ~~complex-hybrid~~ Walsh orthogonal code matrix
 = N rows of N chip code vectors
 = [$\tilde{W}(u)$] matrix of row vectors $\tilde{W}(u)$
 = [$\tilde{W}(u, n)$] matrix of elements $\tilde{W}(u, n)$
 $\tilde{W}(u) =$ ~~Complex-Hybrid~~ Walsh code vector u
 = [$\tilde{W}(u, 0), \tilde{W}(u, 1), \dots, \tilde{W}(u, N-1)$]
 $\tilde{W} = +/-1 \quad +/-j$ possible value

We start by constructing the complex Walsh dc code vector $\tilde{W}(0)$. We use equation $E(0) = C(0)$ in 43 in equations (7),

the correspondence in equations (6), and observe that the dc ~~complex-hybrid~~ Walsh vector has both real and imaginary components in the \tilde{W} domain, to derive the dc ~~complex~~ hybrid Walsh code vector equation:

5

$$\tilde{W}(0) = W(0) + jW(0) \quad \text{for } u=0 \quad (11)$$

10 For ~~complex-hybrid~~ Walsh code vectors $\tilde{W}(u)$, $u=1,2,\dots,N/2-1$, we start with the Walsh code properties in (5),(6) and apply the correspondences in equations (10) between the ~~complex-hybrid~~ Walsh and DFT bases, to the DFT equations 43 in equations (7)+ to derive the equations:

15

$$\begin{aligned} \tilde{W}(u) &= W_e(u) + jW_o(u) && \text{for } u=1,2,\dots,N/2-1 && (12) \\ &= W(2u) + jW(2u-1) && \text{for } u=1,2,\dots,N/2-1 \end{aligned}$$

20 For ~~complex-hybrid~~ Walsh code vector $\tilde{W}(N/2)$ we use the equation $E(N/2)=C(N/2)$ 43 in equations (7) and the same rationale used to derive equation (11), to ~~yield-derive~~ the equation: ~~for~~

$$\tilde{W}(u) = W(N-1) + jW(N-1) \quad \text{for } u=N/2 \quad (13)$$

25 For ~~complex-hybrid~~ Walsh code vectors $\tilde{W}(N/2+\Delta u)$, $\Delta u=1,2,\dots,N/2-1$ we apply the correspondences between the ~~complex-hybrid~~ Walsh and DFT bases to the spectral foldover equation $E(N/2+\Delta u)=C(N/2-\Delta u)-jS(N/2-\Delta u)$ in equations (9) with the changes in indexing required to account for the W indexing in equations (5),(6). The
30 to derive the equations: are

$$\tilde{W}(N/2+\Delta u) = W(N-1-\Delta eu) + W(N-1-\Delta ou) \quad (14)$$

$$\text{for } u=N/2+1, \dots, N-1 \quad (14)$$

$$= W(N-1-2\Delta u) + jW(N-2\Delta u)$$

$$\text{for } u=N/2+1, \dots, N-1$$

5

using the notation $\Delta eiu=2\Delta iu$, $\Delta eio=2\Delta iu-1$. These ~~complex~~ hybrid Walsh code vectors in equations (11), (12), (13), (14) are the equations of definition for the ~~complex~~-hybrid Walsh code

10

vectors. An equivalent way to derive the ~~complex~~-hybrid Walsh code vectors in C^N from the real Walsh basis in R^{2N} is to use a sampling technique which is a known method for deriving a complex

15

basis in C^N from a real basis in R^{2N} .

Transmitter equations (15) describe a representative ~~complex~~-hybrid Walsh CDMA encoding for the transmitter in FIG. 1. It is assumed that there are N ~~complex~~-hybrid Walsh code vectors $\tilde{W}(u)$ 44 which are the ~~each of length N chips similar to the definitions for the real Walsh code vectors 1 in equations (1).~~ The code vector is presented by a $1 \times N$ N-chip row vector $\tilde{W}(u) = [\tilde{W}(u,0), \dots, \tilde{W}(u,N-1)]$ where $\tilde{W}(u,n)$ is chip n of code u. The code vectors are the row vectors of the ~~complex~~-hybrid Walsh matrix \tilde{W} . Walsh code chip n of code vector u has the possible values $\tilde{W}(u,n) = +/-1 +/-j$. Each user is assigned a unique Walsh code which allows the code vectors to be designated by the user symbols $u=0,1,\dots,N-1$ for N ~~complex~~-hybrid Walsh codes. The ~~complex~~-hybrid Walsh code vectors $\tilde{W}(u)$ derived in

20

25

30

equations (11), (12), (13), (14) are summarized 44 in terms of their real and imaginary component code vectors $\tilde{W}(u) = W_R(u) + jW_I(u)$ where $W_R(u)$ and $W_I(u)$ are respectively the real and imaginary component code vectors. As per the derivation of $\tilde{W}(u)$ the sets

of real axis code vectors $\{W_R(u)\}$ and the imaginary axis code vectors $\{W_I(u)\}$ both consist of the ~~real~~ Walsh code vectors in R^N with the ordering modified to ensure that the definition of the ~~complex-hybrid~~ Walsh vectors satisfies equations (11), (12), (13), (14).

~~Complex-Hybrid~~ Walsh CDMA encoding for transmitter (15)

44 ~~Complex-Hybrid~~ Walsh codes use the definitions

10 ~~for the real Walsh codes in 1 equations (1) and the definitions of the complex Walsh codes in equations defined in (11), (12), (13), (14) We find~~

~~\tilde{W} = complex Walsh $N \times N$ orthogonal code matrix consisting of N rows of N chip code vectors~~

15 ~~= $[\tilde{W}(u)]$ matrix of row vectors $\tilde{W}(u)$~~

~~= $[\tilde{W}(u,n)]$ matrix of elements $\tilde{W}(u,n)$~~

$\tilde{W}(u)$ = ~~complex-Hybrid~~ Walsh code vector u
 $= W_R(u) + jW_I(u)$ for $u=0,1,\dots,N-1$

where

20 $W_R(u) = \text{Real}\{ \tilde{W}(u) \}$
 $= W(0)$ for $u=0$
 $= W(2u)$ for $u=1,2,\dots,N/2-1$
 $= W(N-1)$ for $u=N/2$
 $= W(2N-2u-1)$ for $u=N/2+1,\dots,N-1$

25 $W_I(u) = \text{Imag}\{ \tilde{W}(u) \}$
 $= W(0)$ for $u=0$
 $= W(2u-1)$ for $u=1,2,\dots,N/2-1$
 $= W(N-1)$ for $u=N/2$
 $= W(2N-2u)$ for $u=N/2+1,\dots,N-1$

30 $\tilde{W}(u,n)$ = ~~complex-Hybrid~~ Walsh code u chip n
 $= +/-1 +/-j$ possible values

45 Data symbols

$Z(u)$ = Complex data symbol for user u
 $= R(u) + jI(u)$

46 ~~Complex-Hybrid~~ Walsh encoded data

$$\begin{aligned} Z(u,n) &= Z(u) \tilde{W}(u,n) \\ &= Z(u) [\text{sgn}\{W_R(u,n)\} + j\text{sgn}\{W_I(u,n)\}] \\ &= [R(u)\text{sgn}\{W_R(u,n)\} - I(u)\text{sgn}\{W_I(u,n)\}] \\ &\quad + j[R(u)\text{sgn}\{W_I(u,n)\} + I(u,n)\text{sgn}\{W_R(u,n)\}] \end{aligned}$$

10 47 PN scrambling

~~$P_R(n)$ = Chip n of the PN code for the real axis~~

~~$P_I(n)$ = Chip n of the PN code for the imaginary axis~~

$$\begin{aligned} Z(n) &= \text{PN scrambled complex Walsh encoded data chips after summing over the users} \\ &= \sum_u Z(u,n) P_2(n) [P_R(n) + j P_I(n)] \\ &= \sum_u Z(u,n) \text{sgn}\{P_2(n)\} [\text{sgn}\{P_R(n)\} + j \text{sgn}\{P_I(n)\}] \\ &= \text{Complex-Hybrid Walsh CDMA encoded chips} \end{aligned}$$

20

User data symbols 45 are the set of complex symbols $\{Z(u), u=0,1,\dots,N-1\}$. These data symbols are encoded by the hybrid Walsh CDMA codes 46. ~~Each of the user symbols $Z(u)$ is assigned a~~

~~unique complex Walsh code $\tilde{W}(u) = W_R(u) + jW_I(u)$. Complex Walsh encoding of each user data symbol generates an N chip sequence with each chip in the sequence consisting of the user data symbol with the complex sign of the corresponding complex Walsh code chip, which means each encoded chip = [Data symbol $Z(u)$] \times [Sign of $W_R(u) + j$ sign of $W_I(u)$].~~

25 The complex Walsh encoded data symbols are summed and encoded with PN scrambling codes comprising both long and short codes 47, and summed over the users to yield the. complex hybrid Walsh CDMA encoded chips $Z(n)$. ~~These PN codes are~~

defined ~~4~~ in equations ~~(1)~~ as a complex PN for each chip n , equal to $[P_R(u) + j P_I(u)]$ where $P_R(u)$ and $P_I(u)$ are the respective PN scrambling codes for the real and imaginary axes. Encoding with the complex PN is the same as given ~~4~~ in equations ~~(1)~~ for complex data symbols. Each complex Walsh encoded data chip $Z(u,n)$ ~~46~~ is summed over the set of users $u=0,1,\dots,N-1$ and complex PN encoded to yield the complex Walsh CDMA chips $Z(n) = \sum_u Z(u,n) P_2(n) [P_R(n) + j P_I(n)]$ ~~47~~. Combinations of both real and complex data symbols can be used similar to the approach for the real Walsh in equations ~~(1)~~.

Although not considered in this example, it is possible to use combinations of both complex and real data symbols similar to the approach for real Walsh CDMA encoding in equations ~~(1)~~ since the complex Walsh code vectors are the real Walsh code vectors along the real axis and a reordering of the real Walsh code vectors along the imaginary axis.

Receiver equations ~~(16)~~ describe a representative complex hybrid Walsh CDMA decoding for the receiver in FIG. 3. The receiver front end ~~48~~ provides estimates $\{\hat{Z}(n)\}$ of the transmitted complex Walsh CDMA encoded chips $\{Z(n)\}$ for the complex data symbols $\{Z(u)\}$. Orthogonality property ~~49~~ is expressed as a matrix product of the complex hybrid Walsh code chips or equivalently as a matrix product of the complex hybrid Walsh code chip numerical signs of the real and imaginary components. The 2-phase PN codes ~~50~~ have the useful decoding property that the square of each code chip is unity which is equivalent to observing that the square of each code chip numerical sign is unity. Decoding algorithms ~~51~~ perform the inverse of the signal processing for the encoding in equations

(15) to recover estimates $\{\hat{Z}(u)\}$ of the transmitter user symbols $\{Z(n)\}$ for the complex data symbols $\{Z(u)\}$. Combinations of both real and complex data symbols can be used similar to the approach for the real Walsh in equations (2).

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~~Complex-Hybrid~~ Walsh CDMA decoding for receiver (16)

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48 Receiver front end in FIG. 3 provides estimates

$\{\hat{Z}(n)\}$ 28 of the encoded transmitter chip symbols $\{Z(n)\}$ 47 in equations (15).

49 Orthogonality property of ~~complex~~ Walsh NxN matrix \tilde{W}

$$\sum_n \tilde{W}(\hat{u}, n) \tilde{W}'(n, u) =$$

15

$$\sum_n [\text{sgn}\{W_R(\hat{u}, n)\} + j \text{sgn}\{W_I(\hat{u}, n)\}] [\text{sgn}\{W_R(n, u) - j \text{sgn}\{W_I(n, u)\}]$$

$$= 2N \delta(\hat{u}, u)$$

where $\delta(\hat{u}, u)$ = Delta function of \hat{u} and u

$$= 1 \quad \text{for } \hat{u} = u$$

$$= 0 \quad \text{otherwise}$$

20

~~50PN decoding property~~

$$\frac{P(n)P(n)}{\text{sgn}\{P(n)\} \text{sgn}\{P(n)\}} = 1$$

51 Decoding algorithm

$$\hat{Z}(u) =$$

25

$$4^{-1} N^{-1} \sum_n \hat{Z}(n) \text{sign}\{P_2(n)\} [\text{sign}\{P_R(n)\} - j \text{sign}\{P_I(n)\}]^* [\text{sign}\{W_R(n, u)\} - j \text{sign}\{W_I(n, u)\}]$$

= Receiver estimate of the transmitted ~~data~~ data symbol

~~—~~ $Z(u)$ 45 in equations (15)

Although not considered in this example, it is possible to use combinations of both complex and real data symbols similar to the approach for real Walsh CDMA decoding in FIG. 4 since the complex Walsh code vectors are the real Walsh code vectors along the real axis and a reordering of the real Walsh code vectors along the imaginary axis

FIG. 6 ~~complex~~ hybrid Walsh CDMA encoding is a representative implementation of the ~~complex~~ hybrid Walsh CDMA encoding which will replace the current real Walsh encoding 13 in FIG. 1 and is defined in equations (15). Inputs are the user data symbols $\{Z(u)\}$ 52. Encoding of each user by the corresponding ~~complex~~ hybrid Walsh code implements the hybrid Walsh encoding in 46 in equations (15). ~~is described in 53 by the implementation of transferring the sign $\pm 1 \pm j$ of each complex Walsh code chip to the user data symbol followed by a 1-to-N expander $1 \uparrow N$ of each data symbol into an N chip sequence using the sign transfer of the complex Walsh chips. The sign-expander operation 53 generates the N-chip sequence~~

$$Z(u, n) = Z(u) \{ \text{sgn}\{W_R(u, n)\} + j \text{sgn}\{W_I(u, n)\} \} = Z(u) \{ W_R(u, n) + j W_I(u, n) \}$$
for $n=0, 1, \dots, N-1$ for each user $u=0, 1, \dots, N-1$.

This ~~complex~~ Walsh encoding serves to spread each user data symbol into an orthogonally encoded chip sequence which is spread over the CDMA communications frequency band. The ~~complex~~ Walsh encoded Encoded chip sequences for each of the user data symbols are summed over the users 54 followed by PN encoding with long and short codes the scrambling sequence $\{P_R(n) - j P_I(n)\}$ 55. PN encoding is implemented by transferring the sign of each PN chip to the summed chip of the Walsh encoded data symbols. Output is the stream of complex CDMA encoded chips $\{Z(n)\}$ 56. Combinations of both real and complex data symbols can be used similar to the approach for the real Walsh in FIG. 2.

Although not considered in this example, it is possible to use combinations of both complex and real data symbols similar to the approach for real Walsh CDMA encoding in FIG. 2 since the complex Walsh code vectors are the real Walsh code vectors along the real axis and a reordering of the real Walsh code vectors along the imaginary axis.

It should be obvious to anyone skilled in the communications art that this example implementation in FIG. 6 clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.

FIG. 7 complex-hybrid Walsh CDMA decoding is a representative implementation of complex-hybrid Walsh CDMA decoding which will replace the current real Walsh decoding in FIG. 3, and is defined in equations (15). Inputs are the received estimates of the complex CDMA encoded chips $\{\hat{Z}(n)\}$. The PN scrambling code is stripped off from these chips by changing the sign of each chip according to the numerical sign of the real and imaginary components of the complex conjugate of the PN code as per using the decoding algorithms in equations (16).

The complex-hybrid Walsh channelization coding is removed by a pulse compression operation consisting of multiplying each received chip by the numerical sign of the corresponding complex Walsh chip for the user and the output scaled by $1/4N$, and summing the products over the N Walsh chips to recover estimates $\{\hat{Z}(u)\}$ of the user complex data symbols $\{Z(u)\}$. Combinations of both real and complex data symbols can be used similar to the approach for the real Walsh in FIG. 4.

Although ~~not considered in this example, it is possible to use combinations of both complex and real data symbols similar to the approach for real Walsh CDMA decoding in FIG. 4 since the complex Walsh code vectors are the real Walsh code vectors along the real axis and a reordering of the real Walsh code vectors along the imaginary axis.~~

It should be obvious to anyone skilled in the communications art that this example implementations in FIG. 6, 7 clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.

For cellular applications the transmitter description describes the transmission signal processing applicable to this invention for both the hub and user terminals, and the receiver describes the corresponding receiving signal processing for the hub and user terminals for applicability to this invention.

Consider ~~Complex-complex~~ orthogonal CDMA code space C^N for generalized ~~hybrid complex~~ Walsh codes. ~~The power of 2 code lengths $N=2^M$ where M is an integer, for complex Walsh can be modified to which~~ allow the code length N to be a product of powers of primes in equations (17) or a sum of powers of primes in equations (17), at the implementation cost of introducing multiply operations into the CDMA encoding and decoding. In the previous disclosure of this invention we ~~used the~~ N was assumed to be equal to a power of 2 which means $N=2^m$ corresponding to prime $p_0=2$ and integer $M=m_0$. This restriction was made for convenience in explaining the construction of the ~~complex-hybrid~~ Walsh and is not required since it is well known that Hadamard matrices exist for non-

integer powers of 2 and, therefore, ~~complex-hybrid~~ Walsh matrices exist for non-integer powers of 2.

5 Length N of generalized hybrid Walsh ~~hybrid-complex~~ codes (17)

60 Kronecker or tensor product code construction

$$N = \prod_k p_k^{m_k}$$

$$= \prod_k N_k$$

where

p_k = prime number indexed by k starting with k=0

m_k = order of the prime number p_k

N_k = Length of code for the prime p_k

$$= p_k^{m_k} p_k^{m_k}$$

61 Direct sum code construction

$$N = \sum_k p_k^{m_k}$$

$$= \sum_k N_k$$

Add-only arithmetic operations are required for encoding and decoding both real Walsh and ~~complex-hybrid~~ Walsh CDMA codes since the real Walsh values are ± 1 and the ~~complex-hybrid~~ Walsh values are $\{ \pm 1, \pm j \}$ or equivalently are $\{ 1, j, -1, -j \}$ under a -90 degree rotation and normalization which means the only operations are sign transfers and adds plus subtracts or add-only algebraic operations. Multiply operations are more complex to implement than add operations. However, the advantages of having greater flexibility in choosing the orthogonal CDMA code lengths N using equations (17) can offset the expense of multiply operations for particular applications.

Accordingly, this invention includes the concept of generalized hybrid ~~hybrid complex~~ Walsh orthogonal CDMA codes with the flexibility to meet these needs. This extended class of ~~complex hybrid~~ Walsh codes are hybrid in that their construction supplements the ~~complex hybrid~~ Walsh codes with the use of by combining with Hadamard, ~~(or real Walsh)~~, DFT, and other orthogonal codes as well as with quasi-orthogonal PN by relaxing the orthogonality property to quasi-orthogonality.

Generalized ~~hybrid complex~~ Walsh orthogonal CDMA codes can be constructed as demonstrated in 64 and 65 in equations (18) for the Kronecker or tensor product, and in 66 ~~in equations (18)~~ for the direct sum. ~~Code~~ The example code matrices considered for orthogonal CDMA codes in 62 in equations (18) for the construction of the generalized hybrid ~~complex~~ Walsh are the DFT E and Hadamard H or equivalently Walsh W, in addition to the ~~complex hybrid~~ Walsh \tilde{W} . The algorithms and examples for the construction start with the definitions 63 of the $N \times N$ orthogonal code matrices $\tilde{W} = \tilde{W}_N, \dots, E = E_N, H = H_N$ ~~for \tilde{W}, E, H~~ respectively, ~~examples for low orders $N=2, 4, \dots$ and the~~ equivalence of E_4 and \tilde{W}_4 after the \tilde{W}_4 is rotated through the angle -90-45 degrees and rescaled. The CDMA current and developing standards use the prime 2 which generates a code length $N=2^M$ where $M=\text{integer}$. For applications requiring greater flexibility in code length N , additional primes can be used using the ~~Kronecker tensor~~ construction. ~~We~~ This flexibility is illustrated this in 65 with the addition of prime=3. The use of prime=3 in addition to the prime=2 in the range of $N=8$ to $N=64$ is observed to increase the number of N choices ~~from 4 to 9~~ at a modest cost penalty of using multiples of the angle increment 30 degrees for prime=3 in addition to the angle increment 90 degrees for prime=2. As noted in 65 there are several choices in the ordering of the ~~Kronecker tensor~~ product construction and 2 of

these choices are used in the construction- and these choices yield different sets of orthogonal codes.

Direct sum construction provides greater flexibility in the choice of N without necessarily introducing a multiply penalty.

5 However, the addition of the zero matrix in the construction is generally not desirable for CDMA communications.

10

Construction of generalized hybrid ~~hybrid-complex~~ Walsh
orthogonal codes (18)

62 Code matrices

15 \tilde{W}_N = NxN ~~complex-hybrid~~ Walsh ~~orthogonal~~-code matrix

E_N = NxN DFT ~~orthogonal~~-code matrix

H_N = NxN Hadamard ~~orthogonal~~-code matrix

20

63 Low-order code definitions and equivalences

$$2 \times 2 \quad H_2 = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$= E_2$$

25

$$= (e^{-j\pi/4} / \sqrt{2}) * \tilde{W}_2$$

30

$$3 \times 3 \quad E_3 = \begin{bmatrix} 1 & 1 & 1 \\ 1 & e^{j2\pi/3} & e^{j2\pi/3} \\ 1 & e^{j2\pi/3} & e^{j2\pi/3} \end{bmatrix}$$

$$4 \times 4 \quad H_4 = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix}$$

$$\tilde{W}_4 = \begin{bmatrix} 1+j & 1+j & 1+j & 1+j \\ 1+j & -1+j & -1-j & 1-j \\ 1+j & -1-j & 1+j & -1-j \\ 1+j & 1-j & -1-j & -1+j \end{bmatrix}$$

$$E_4 = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & j & -1 & -j \\ 1 & -1 & 1 & -1 \\ 1 & -j & -1 & j \end{bmatrix}$$

$$= (e^{-j\pi/4} / \sqrt{2}) \tilde{W}_4$$

64 Kronecker or tensor product construction for $N = \prod_k N_k$

Code matrix $C_N = N \times N$ ~~hybrid-orthogonal~~ generalized
hybrid Walsh CDMA code matrix
 Kronecker or tensor product construction of C_N

$$\underline{C}_N = C_0 \prod_{k>0} \otimes C_{N_k}$$

Kronecker or tensor product definition

$A = N_a \times N_a$ orthogonal code matrix $[a_{ik}]$

$B = N_b \times N_b$ orthogonal code matrix

$A \otimes B =$ Kronecker or tensor product of matrix A

and matrix B

= $N_a N_b \times N_a N_b$ orthogonal code matrix consisting
of the elements $[a_{ik}]$ of matrix A multiplied
by the matrix B

$$= [a_{ik} B]$$

65 Kronecker or tensor product construction examples for
primes $p=2,3$ and the range of sizes $8 \leq N \leq 64$

$$8 \times 8 \quad C_8 = \tilde{W}_8$$

$$12 \times 12 \quad C_{12} = \tilde{W}_4 \otimes E_3$$

$$C_{12} = E_3 \otimes \tilde{W}_4$$

$$16 \times 16 \quad C_{16} = \tilde{W}_{16}$$

$$18 \times 18 \quad C_{18} = \tilde{W}_2 \otimes E_3 \otimes E_3$$

$$C_{18} = E_3 \otimes E_3 \otimes \tilde{W}_2$$

$$24 \times 24 \quad C_{24} = \tilde{W}_8 \otimes E_3$$

$$C_{24} = E_3 \otimes \tilde{W}_8$$

$$32 \times 32 \quad C_{32} = \tilde{W}_{32}$$

$$36 \times 36 \quad C_{36} = \tilde{W}_4 \otimes \tilde{W}_3 \otimes \tilde{W}_3$$

$$C_{36} = \tilde{W}_3 \otimes \tilde{W}_3 \otimes \tilde{W}_4$$

$$48 \times 48 \quad C_{48} = \tilde{W}_{16} \otimes \tilde{W}_3$$

$$C_{48} = \tilde{W}_3 \otimes \tilde{W}_{16}$$

$$64 \times 64 \quad C_{64} = \tilde{W}_{64}$$

66 Direct sum construction for $N = \sum_k N_k$

Code matrix $C_N = N \times N$ hybrid orthogonal CDMA code matrix

Direct sum construction of C_N

$$C_N = C_0 \prod_{k>0} \oplus C_{N_k}$$

Direct sum definition

$A = N_a \times N_a$ orthogonal code matrix

$B = N_b \times N_b$ orthogonal code matrix

$A \oplus B =$ Direct sum of matrix A and matrix B

$= N_a + N_b \times N_a + N_b$ orthogonal code matrix

$$= \begin{bmatrix} A & O_{N_a \times N_b} \\ O_{N_b \times N_a} & B \end{bmatrix}$$

where $O_{N_1 \times N_2} = N_1 \times N_2$ zero matrix

It should be obvious to anyone skilled in the communications art that ~~this~~ these example implementations of the generalized hybrid ~~hybrid complex~~ Walsh in equations (18) clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches. For example, the Kronecker or tensor product matrices E_N and H_N can be replaced by functionals.

For cellular applications the transmitter description which includes equations (18) describes the transmission signal processing applicable to this invention for both the hub and user terminals, and the receiver corresponding to the decoding of equations (18) describes the corresponding receiving signal processing for the hub and user terminals for applicability to this invention.

Consider ~~Computationally~~ computationally efficient encoding and decoding of complex Walsh CDMA codes and hybrid complex Walsh CDMA codes. ~~It is well known that fast and efficient encoding and decoding algorithms exist for the real Walsh CDMA codes. These are documented in reference [6].~~ It is obvious that with suitable modifications these algorithms can be used to develop fast and efficient encoding and decoding algorithms for the ~~complex-hybrid~~ Walsh CDMA codes since these complex codes have real and imaginary code vectors which are from the same set of real Walsh CDMA codes.

It is well known that the Kronecker or tensor product construction involving DFT, H and real Walsh orthogonal code vectors have efficient encoding and decoding algorithms. It is obvious that with suitable modifications these algorithms can be used to develop fast and efficient encoding and decoding algorithms for the Kronecker or tensor products of DFT, H and ~~complex-hybrid~~ Walsh CDMA codes since these ~~complex-hybrid~~ Walsh codes have real and imaginary code vectors which are from the same set of real Walsh CDMA codes. It is obvious that fast and efficient encoding and decoding algorithms exist for direct sum construction and functional combining.

Preferred embodiments in the previous description is provided to enable any person skilled in the art to make or use the present invention. The various modifications to these embodiments will be readily apparent to those skilled in the art, and the generic principles defined herein may be applied to other embodiments without the use of the inventive faculty. Thus, the present invention is not intended to be limited to the embodiments shown herein but is ~~not~~ to be accorded the wider scope consistent with the principles and novel features disclosed herein.

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5 Generation Mobile Systems in Europe"~~

~~{3} TIA/EIA interim standard, TIA/EIA/IS-95-A, May 1995~~

~~{4} United States Patent 5,715,236 Feb. 3 1998, "System and
method for generating signal waveforms in a CDMA cellular
telephone system"~~

~~{5} United States Patent 5,943,361 Aug 24 1999, "System and
10 method for generating signal waveforms in a CDMA cellular
telephone system"~~

~~{6} K.G. Beauchamp's book "Walsh functions and their
Applications", Academic Press 1975~~

DRAWINGS AND PERFORMANCE DATA



FIG. 1 CDMA Transmitter Block Diagram

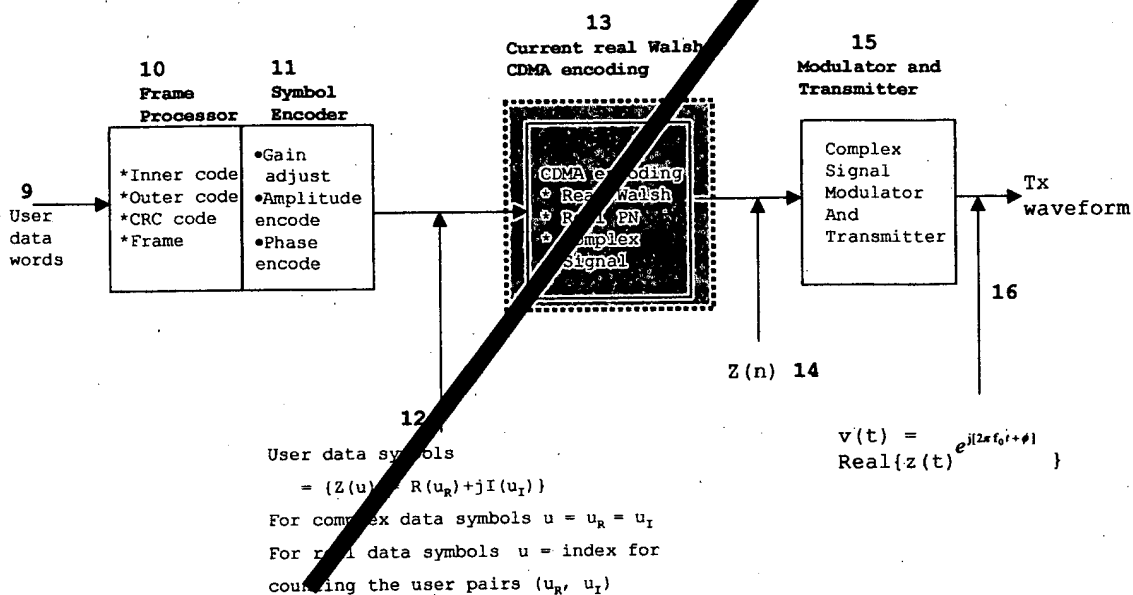
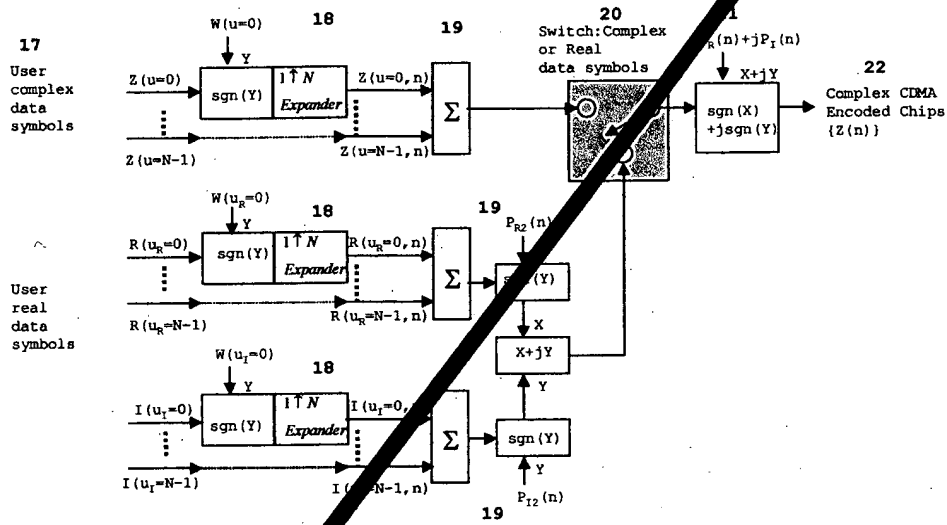


FIG. 2 Real Walsh CDMA Encoding



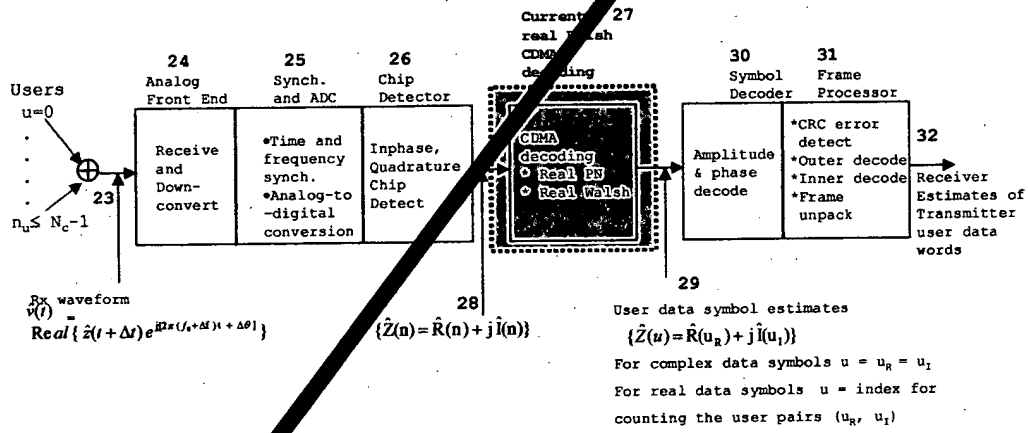
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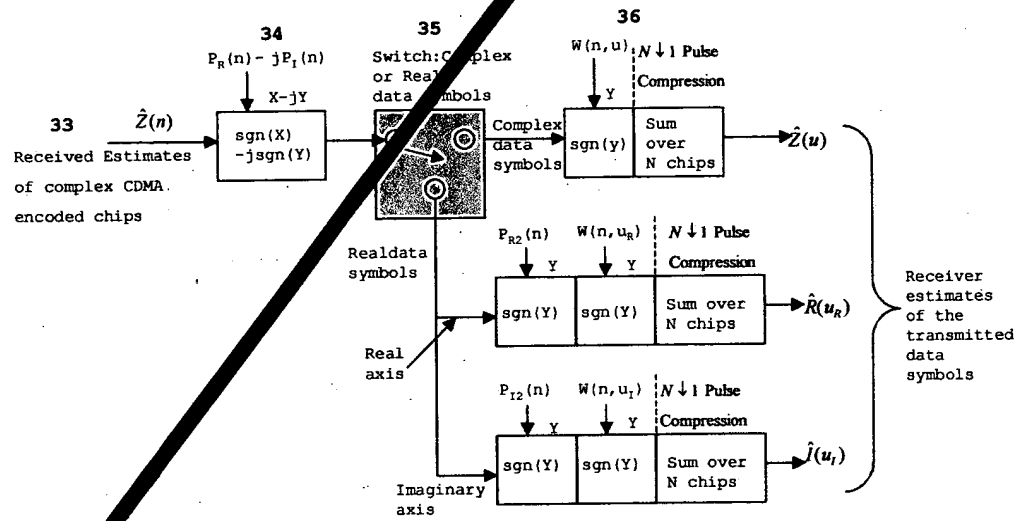
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FIG. 3 CDMA Receiver Block Diagram



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FIG. 4 Real Walsh CDMA Decoding

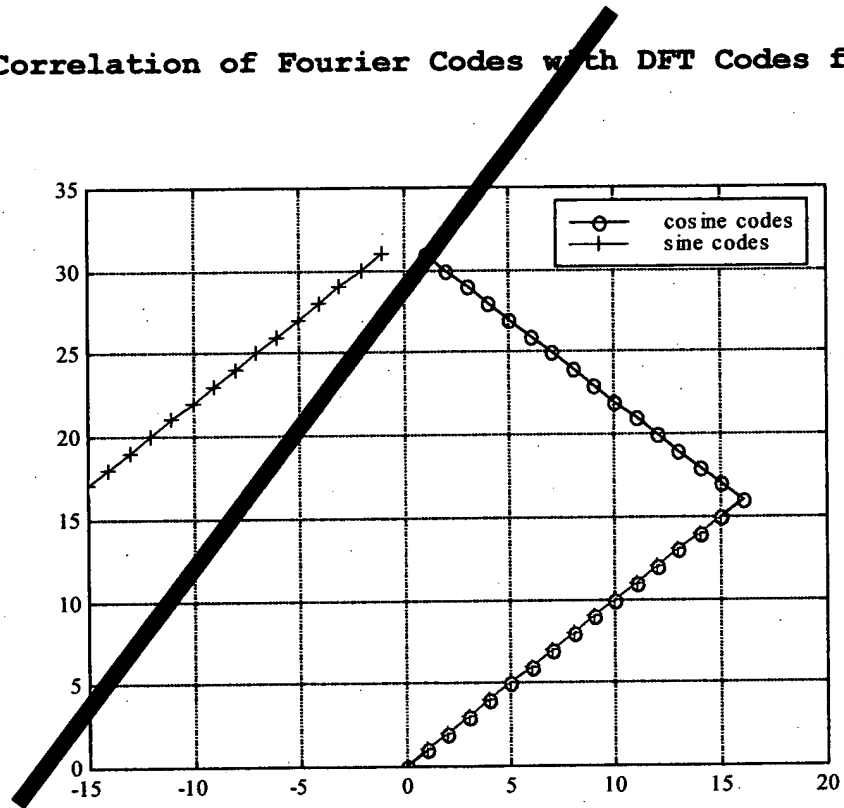


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FIG. 5 Correlation of Fourier Codes with DFT Codes for N=32



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FIG. 6 Complex Walsh CDMA Encoding

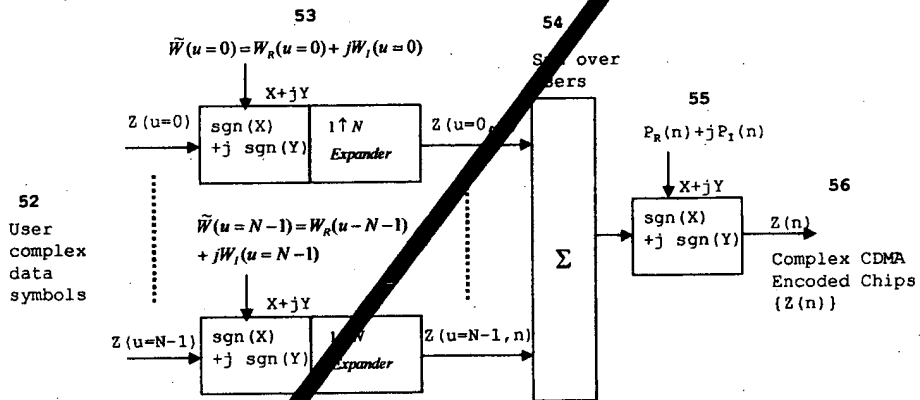


FIG. 7 Complex Walsh CDMA Decoding

